Three-Dimensional Spatiotemporal Pulse-Train Solitons

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Experimental realization of three-dimensional spatiotemporal solitons, which were proposed several decades ago, is still considered a “grand challenge” in nonlinear science. Here, we present experimental observation of 3D optical spatiotemporal pulse-train solitons. A spatially bright temporally dark pulse-train beam is trapped in a bulk medium that supports two types of nonlinearities: slowly responding saturable self-focusing that collectively self-trap the beam in the transverse directions and fast self-phase modulation that self-localizes each dark notch temporally (longitudinally). This work opens the possibility for experimental investigations of various soliton phenomena, including soliton interaction in 3D, formation of multimode spatiotemporal solitons, and envisioning new entities like partially coherent spatiotemporal solitons.

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Solitons are self-trapped wave packets for which nonlinearity robustly balances linear broadening and that exhibit particlelike properties [1,2]. Solitons that are self-trapped in one or two dimensions (in space or time) have been observed in many systems, including shallow [3] and deep [4] water waves, the nervous system [5], meteorology [6], Bose-Einstein condensates [7,8], and optics [9–12]. Three-dimensional spatial solitons were only recently observed in chiral ferromagnetic liquid crystal colloids [13,14].

In addition to spatial and temporal solitons, solitons can also be trapped in both space and time, simultaneously [15]. Since the proposal of optical spatiotemporal solitons (STS), almost three decades ago [16], they have evolved into a vibrant field of research that combines spatial, temporal, and nonlinear optics [17–20]. 3D STS, which are also termed “light bullets,” have particularly been attracting substantial theoretical interest in both fundamental [17,21,22] and applied science [23,24]. The experimental progress, on the other hand, has been quite limited. The main challenges include the matching of the diffraction and dispersion lengths, which should be balanced simultaneously by the nonlinearity, and stability to noise, which is especially challenging for high-dimensional solitons [16–20]. Spatiotemporal solitons

were first demonstrated experimentally in 1999 by employing the cascaded second harmonic generation process in bulk medium [25]. However, these solitons are fundamentally two dimensional; i.e., they are trapped in time and in only one spatial transverse direction while they are very wide and spectrally dispersed in the other transverse direction. The propagation distance of these solitons is limited by transverse instability. More recently, quasi-3D STS were experimentally demonstrated in an array of waveguides with Kerr nonlinearity [26,27]. These discrete light bullets (LBs) propagated with approximately stationary pulse width for about two diffraction lengths. The higher-order nonlinear effects, that lead to spectral redshift, upsets the balance between the wavelength-sensitive discrete diffraction and self-focusing effects and eventually results in the disintegration of these LBs. Early this year, mode-locked spatial cavity solitons with pulse duration shorter than the cavity round-trip were observed [28]. This research direction may enable generation of bright 3D cavity solitons. Linear light bullets employing the nondiffraction property of Airy and Bessel beams were demonstrated [29,30]. Still, stable 3D STS (that can support solitons interactions) have not been experimentally demonstrated. Whilst in optical lattices quasi 3D STS were observed, no similar progress has been made in homogeneous media.

In 2009, spatiotemporal pulse-train solitons (STPTSs) were proposed, offering a new path toward generation of 3D STS [31,32]. A STPTS consists of a sequence of short pulses that are collectively trapped in the transverse directions by a slow self-focusing mechanism and, simultaneously, each pulse is self-trapped temporally by a fast self-phase modulation (e.g., induced by the Kerr nonlinearity). The response time of the slow self-focusing is

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FIG. 1. Experimental setup. A Ti:sapphire laser pulse-train beam ($\lambda = 0.8 \mu\text{m}$) with 1-KHz repetition rate and 30-fs pulse duration is divided into reference and signal beams. The signal beam propagates through a pulse shaper designed to form a dark pulse (100-fs FWHM) centered at a relatively wide background pulse (1-ps FWHM). The dark pulse-train beam is then focused to the input face of a photorefractive SBN crystal ($5 \times 5 \times 15 \text{ mm}$ and $6 \times 6 \times 6 \text{ mm}$). The spatial intensity distributions at the input and output faces of the crystal are recorded by an imaging system and CCD. The temporal pulse profile is characterized through spectral interferometry by interfering the reference and signal beams in a spectrometer.

much longer than the time interval between consecutive pulses, hence, it is affected by the averaged power of the beam; i.e., it is insensitive to the temporal profile of the pulses. The characteristic lengths of the slow and fast nonlinearities are tuned to match the diffraction and dispersion lengths, respectively. For stability, the slow self-focusing should be nonlocal or saturable and significantly larger than the fast nonlinearity. Two types of STPTSs were predicted in Refs. [31,32]. In one type, the STPTSs are bright (i.e., their profiles are bell-like) in

all directions, while in the other type they are dark in the time domain (a dark soliton is a self-localized intensity dip embedded in a continuous background [33]). Fully bright STPTSs can exist in anomalous dispersive media while spatially bright temporally dark STPTSs require normal dispersion. Following Refs. [31,32], the two-nonlinearity approach was employed for predicting generation of dense LB trains [34] and experimental demonstrations of third-harmonic generation [35] and spectral broadening [36] within 2D spatial solitons.

FIG. 2. Three-dimensional spatiotemporal pulse-train soliton in a long crystal ($L = 15 \text{ mm}$). (a) Spatial intensity distribution at the input plane of the crystal ($\text{FWHM} \approx 15 \mu\text{m}$). (b) The intensity distribution at the output plane of the crystal under approximately linear propagation condition (the screening self-focusing is turned off by applying zero external voltage and the Kerr nonlinearity is small because the intensity of the beam is low— $10 \mu\text{W}$ averaged power of the incoming beam). The beam broadens to $\text{FWHM} \approx 278 \mu\text{m}$. Output plane intensity distributions when the screening self-focusing is turned on ($V = 500 \text{ V}$) at (c) $10 \mu\text{W}$ and (d) $70 \mu\text{W}$ averaged powers, demonstrating the transverse spatial self-trapping ($\text{FWHM} \approx 29 \mu\text{m}$ and $\text{FWHM} \approx 19 \mu\text{m}$, respectively). (e) Reconstructed intensity pulse profiles of (bottom up) input pulse (black), diffracted beam with $P_{\text{avg}} = 10 \mu\text{W}$ (red), and spatially trapped beam with $P_{\text{avg}} = 10, 20, 25, 30, 40, 45, 50, 60$, and $70 \mu\text{W}$. (f) The duration of the dark notch as a function of average power demonstrating the temporal confinement. The horizontal dashed line corresponds to the duration at the input plane.

FIG. 3. Three-dimensional spatiotemporal pulse-train soliton in a short crystal ($L = 6$ mm). (a) Spatial intensity distribution at the input plane of the crystal (FWHM ≈ 15 μm). (b) The intensity distribution at the output plane of the crystal under approximately linear propagation condition. The beam broadens to FWHM ≈ 136 μm . Output plane intensity distributions when the screening self-focusing is turned on ($V = 1800$ V) at (c) 10 μW and (d) 60 μW averaged powers, demonstrating the transverse spatial self-trapping (FWHM ≈ 26 μm and FWHM ≈ 13 μm , respectively). (e) Reconstructed intensity pulse profiles of (bottom up) input pulse (black), diffracted beam with $P_{\text{avg}} = 10$ μW (red), and spatially trapped beam with $P_{\text{avg}} = 10, 20, 30, 40, 50$, and 60 μW . (f) The duration of the dark notch as a function of average power demonstrating the temporal confinement. The horizontal dashed line corresponds to the duration at the input plane.

Here, we demonstrate experimentally 3D spatiotemporal pulse-train solitons. We observe solitonic propagation for 29 diffraction lengths and approximately two dispersion lengths, limited by the finite length of our crystals. Thus, investigations of 3D soliton interactions and other new phenomena should be accessible in this system. Our approach for experimentally generating STPTSs is to utilize the screening self-focusing in photorefractives [37]. This self-focusing is highly saturable; hence, it can support high-dimensional solitons [2] and is also very slow—its response time can be many seconds and even minutes, a feature that is utilized for generation of incoherent solitons [2]. Specifically, we use a strontium barium niobate (SBN) photorefractive crystal that was shown to support 2D spatial solitons of picosecond [38] and femtosecond [36] pulse-train beams at a wavelength of 0.8 μm . The dispersion of SBN is normal in this wavelength; hence, we generate here spatially bright temporally dark STPTSs.

The experimental setup is shown in Fig. 1. A Ti:sapphire laser beam with 1-KHz repetition rate and 30-fs pulse duration is divided into reference and signal beams. The signal beam propagates through a pulse shaper designed to form a dark pulse whose full width at half of the maximum intensity is 100 fs centered at a relatively wide background pulse (a super-Gaussian with 1 ps FWHM). The pulse-train beam is then focused

on the input face of a photorefractive SBN crystal ($5 \times 5 \times 15$ mm and $6 \times 6 \times 6$ mm, as shown in Figs. 2 and 3, respectively). The spatial intensity distributions at the input and output faces of the crystal are recorded by an imaging system and a CCD. The temporal pulse profile is characterized by spectral interferometry [39] (the reference pulse is characterized by using a frequency-resolved optical gating apparatus [40]).

The strength of the slow photorefractive nonlinearity is controlled via an applied voltage along the c axis of the crystal, which is perpendicular to the propagation direction. The transverse self-trapping is demonstrated in Figs. 2(a)–2(d). Figure 2(a) shows the intensity distribution of the focused beam at the input face of the crystal (FWHM ≈ 15 μm). When the photorefractive nonlinearity is off (zero applied voltage), the beam diffracts significantly after propagating along 15 mm in the SBN crystal [Fig. 2(b)] and reaches a size of FWHM ≈ 278 μm (the observed modulation in the diffracted beam is due to growth-induced “striations” in the crystal [41]). When applying a high voltage (500 V) on the SBN crystal, a spatial self-trapping is achieved [36–38]. Figures 2(c) and 2(d) show the output trapped beam for an average power of 10 and 70 μW , respectively (we do not increase the averaged power beyond 70 μW in order to not damage the crystal). The temporal self-trapping is presented in

Figs. 2(e) and 2(f). Figure 2(e) shows the reconstructed intensity profiles of the input pulse (lowest curve) and the output pulses at various conditions, starting with an average power of $10\ \mu\text{W}$ and no photorefractive nonlinearity ($V = 0$), and then the output pulses with increasing averaged power with the photorefractive nonlinearity turned on. As shown in Fig. 2(f), the duration of the dark notch (determined according to the algorithm for calculating pulse duration described in Sec. 5.4.1 of Ref. [42]) decreases (as the power increases) from a linearly dispersed pulse of 185 fs to the initial input pulse width of 100 fs. This 3D STS propagates for a distance of 15 mm, which corresponds to 29 diffraction lengths and approximately 1.5 dispersion lengths. Such a long propagation distance should make the experimental investigations of collisions and interactions between 3D solitons accessible.

We repeat the measurements with a shorter crystal ($6 \times 6 \times 6\ \text{mm}$) to verify that the 3D soliton wave packet is stationary along the propagation distance. The experimental results are shown in Fig. 3, which has the same structure as Fig. 2. Indeed, it shows that 3D spatiotemporal solitons are formed in the short and long crystals at similar parameters.

In conclusion, we demonstrate experimentally stable 3D spatiotemporal solitons. The experiment is based on utilizing a combination of slow and fast nonlinearities to produce spatiotemporal pulse-train solitons. It should now be possible to explore interactions and collisions between 3D solitons experimentally, some of which are predicted to be unique to 3D solitons [43]. Moreover, new phenomena are expected since STPTSs require both slow and fast nonlinearities. For example, consider interaction between STPTSs that overlap spatially. It will be interesting to explore this interaction as a function of the degree of temporal overlap between the pulses, from full overlap to absent temporal overlap. Also, it should be possible to produce multimode [44] and maybe even partially coherent spatiotemporal pulse-train solitons. An exciting next step is to produce a fully bright 3D STPTS, e.g., by utilizing the slowly responding, nonlocal thermal nonlinearity of fused silica at a spectral region near $2\ \mu\text{m}$, where the dispersion is anomalous [31,32]. Another promising research direction is to exploit the concept of spatiotemporal pulse-train solitons, where the temporal and spatial confinements are largely controlled by different knobs, for improving mode locking of lasers. All in all, we expect that the new experimental platform and high dimensionality will give rise to fundamental and applicable new opportunities in soliton science.

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